



Testing Digital Systems I

Lecture 8: Boolean Testing Using Fault Models (D Algorithm)

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Specific-Fault Oriented Test Generation

- Three Approaches
 - Internal Line Values Assigned (D Algorithm) (Roth-1966)
 - D-cubes
 - Bridging faults
 - Logic gate function change faults
 - Input Values Assigned (PODEM) (Goel – 1981)
 - X-Path-Check
 - Path propagation constraints to limit ATPG search space
 - Backtracing
 - Input and Internal Values Assigned (FAN) (Fujiwara)
 - Efficiently constrained backtarce

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Fault Cone and D-frontier

- Fault Cone
 - Set of hardware affected by fault
- D-frontier
 - Set of gates closest to POs with fault effect(s) at input(s)

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D Algorithm

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D-Algorithm -- Roth IBM (1966)

- Fundamental concepts invented:
 - First complete ATPG algorithm
 - D-Cube
 - D-Calculus
 - Implications – forward and backward
 - Implication stack
 - Backtrack
 - Test Search Space

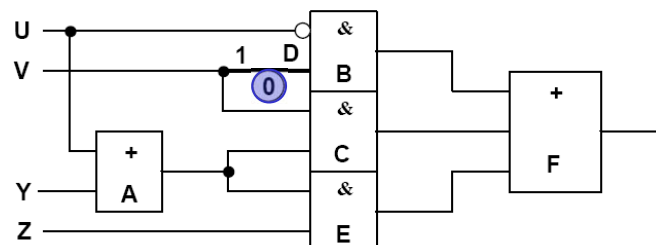
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D Algorithm

- Assigning internal line values
- Example:
 - Test for Stuck-at-0 on Lower Input to Gate B
 - Activate Fault — Put 1 on Faulty Lead



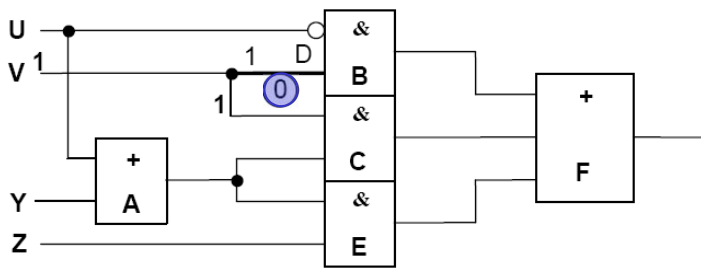
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D Algorithm

- Example
 - Test for Stuck-at-0 on Lower Input to Gate B
- Implication
 - Record Effects of Previous Assignments

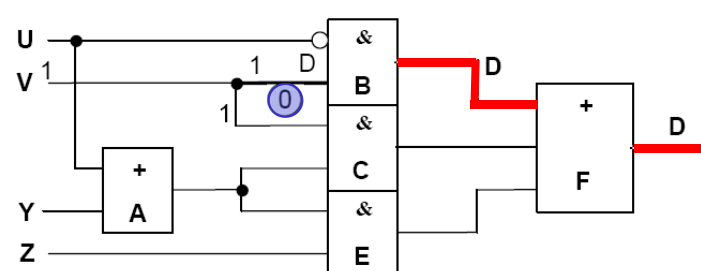


The diagram shows a digital circuit with inputs U, V, Y, and Z. Gate A is an adder (+) with inputs Y and Z. Gate B is an AND (&) gate with inputs U and V. Gate C is an AND (&) gate with inputs V and the output of Gate A. Gate E is an AND (&) gate with inputs U and Z. Gate F is an adder (+) with inputs from Gate B and Gate C. A fault 'D' (stuck-at-0) is indicated on the lower input of Gate B (input V). The value '1' is shown on the upper input of Gate B (input U). A blue circle with '0' is shown on the lower input of Gate B, indicating the fault condition.

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D Algorithm

- Propagation
 - Select Path to Propagate D to Output
 - Single versus Multiple Path Propagation



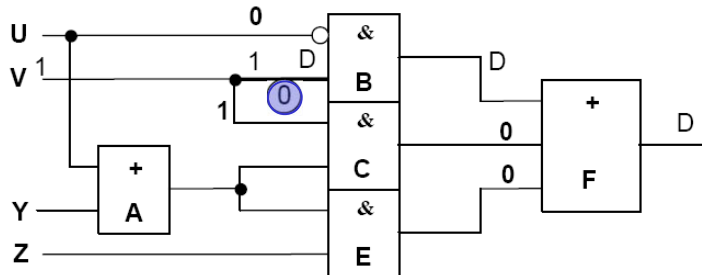
The diagram is identical to the one in slide 7, but it highlights the propagation path of the fault 'D' in red. The path starts at the lower input of Gate B (input V), goes through Gate B, and then through Gate F to the final output. The value '1' is shown on the upper input of Gate B (input U). A blue circle with '0' is shown on the lower input of Gate B, indicating the fault condition.

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D Algorithm

- Propagation

- Assign Required Gate Input Values
- 0s on other inputs of OR, NOR Gates with D or \bar{D} Input
- 1s on other inputs of AND, NAND Gates with D or \bar{D} Input



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Line Justification

- Find Input Assignment to Place Value v on Line g
- Path Tracing Approach
 - Propagate Signals using Element Functions
 - Must Choose Element Input Values and Paths
- Primitive cube of an element (gate) with output Z
 - List of prime implicants of Z and Z'

AND

A	B	Z
1	1	1
0	—	0
—	0	0

NAND

A	B	Z
1	1	0
0	—	1
—	0	1

Implication (no choices)

Decision (choices)

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D Algorithm

- Line Justification
 - Assign Required Gate Input Values
 - 0 on lower input of C to give 0 on output

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D Algorithm

- Implication
 - Record Effects of Previous Assignments
- Test is $U, V, Y, Z = 0, 1, 0, d$
- DIFFICULTY
 - Internal Line Values May be Inconsistent

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D Algorithm

- Example
 - Test for Stuck-at-1 on Gate A Output
- Activate Fault
 - Put 0 on Faulty Lead

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D Algorithm

- Example
 - Test for Stuck-at-1 on Gate A Output
- Implication
 - Record Effects of Previous Assignments

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D Algorithm

- Example
 - Test for Stuck-at-1 on Gate A Output
- Propagation
 - Select Path to Propagate D to Output

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D Algorithm

- Propagation
 - Assign Required Gate Input Values
 - 0s on other inputs of OR, NOR Gates with D or \bar{D} Input
 - 1s on other inputs of AND, NAND Gates with D or \bar{D} Input

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D Algorithm

- Example
 - Test for Stuck-at-1 on Gate A Output
- Implication
 - Record Effects of Previous Assignments

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D Algorithm

- Example
 - Test for Stuck-at-1 on Gate A Output
- Propagation
 - Select Alternate Path to Propagate D to Output

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D Algorithm

- Example
 - Test for Stuck-at-1 on Gate A Output
- Implication
 - Record Effects of Previous Assignments
- Test is $U, V, Y, Z = 0, 0, 0, 1$

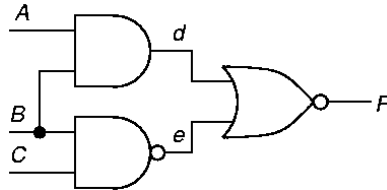
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D Calculus

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Singular Cover

- Singular Cover
 - Minimal set of input signal assignments to show essential prime implicants of Karnaugh map



Gate	Inputs	Output	Gate	Inputs	Output
AND	A B	d	NOR	d C	F
1	0 X	0	1	1 X	0
2	X 0	0	2	X 1	0
3	1 1	1	3	0 0	1

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D Algorithm


- D-Cube
 - A collapsed truth table entry
- Example
 - AND gate

	A	B	d
Rows 1 & 3	D	1	D
Reverse inputs	1	D	D
And two cubes	<u>D</u>	<u>D</u>	<u>D</u>
Interchange D and D	<u>D</u>	<u>D</u>	<u>D</u>
	<u>1</u>	<u>D</u>	<u>D</u>
	<u>D</u>	1	<u>D</u>

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D Algorithm

- D Intersection
 - Defines how different D-cubes can coexist for different gates in logic circuit
 - If one cube assigns a specific signal value, the other cubes must assign either that same value or X
 - $1 \cap 1 = 1 \cap X = X \cap 1 = 1$
 - $0 \cap 0 = 0 \cap X = X \cap 0 = 0$
 - $X \cap X = X$

ψ, ϕ represent incompatible assignments
 μ, λ represent incompatibility if both present

\cap	0	1	X	D	\bar{D}
0	0	ϕ	0	ψ	ψ
1	ϕ	1	1	ψ	ψ
X	0	1	X	D	\bar{D}
\bar{D}	ψ	ψ	\bar{D}	μ	λ
D	ψ	ψ	D	λ	μ

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D Algorithm

- Primitive D-cube of Failure (PDF)
 - Models fault including
 - SA1: represented by \bar{D}
 - SA0: represented by D
 - Example: AND gate
 - PDF for output SA0 is 1 1 D
 - PDFs for output SA1 are 0 X \bar{D} , X 0 \bar{D}
- Propagation D-cube
 - Models conditions under which fault effect propagates through gate

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Implication Procedure

1. Model fault with appropriate PDF
 2. Select propagation D-cubes to propagate fault effect to a PO (**D-drive** procedure)
 3. Select singular cover cubes to justify internal circuit signals (**Consistency** procedure)
- D Algorithm's main problem
 - Selects cubes and singular covers arbitrarily

D Algorithm

