





























c codes for 4	4-bit information words.	clock	¥,	\bigcirc		1	\frown	
formation d ₁ , d ₂ , d ₃ ,)	Code $(v_0, v_1, v_2, v_3, v_4, v_5, v_6)$	Reg 1 R	eq 2	*(+) - ↑	→ Re]> g 3	·(+)- ↑	
000	000000			_'•				
001	0001101							
010	0011010							
011	0010111							
100	0110100	The encoding process						
101	0111001		Register values					
110	0101110	Clock period		2	3	D(x)	V(x)	
111	0100011				-			
000	1101000	0	0	0	0	1	1	
001	1100101	1	1	0	1	1	-	
010	1110010	_	-	-		1	0	
011	1111111	2	1	1	1	0	1	
100	1011100	3	0	1	1	0	1	
101	1010001	-	·	-	-	1	0	
110	1000110	4	1	0	0	0	0	
.111	1001011	5	0	1	0	0	0	
n and an annial — d	$d_1 + d_1 x + d_2 x^2 + d_3 x^3$, i i i i i i i i i i i i i i i i i i i	Č.	-	-	0	0	
a polynomial = d_a		6	0	0	1			
erator polynomia	$1 = 1 + y + y^3$	*				0	1	









	510	e Do	50	u		9							Karlsruhe Institute
		or polyn + x +1	I	l, [lock		Reg 1 Reg 2	+ Reg 3	•	• <u> </u>		(x) I(x)		
The dec	oding	process	with c	orrect i	nform	ation	The dec	oding	g process v	vith e	rroneo	us inf	ormation
Clock period		ister val 2	ues 3	V(x)	B(x)	D(x)	Clock period		Register va 2	dues 3	V(x)	B(x)	D(x)
0	0	0	0	1	0	1	0	0	0	0	1	0	1
1	0	0	1	0	1	1	1	0	0	1	0	1	1
2	0	1	1	1	1	0	2	0	1	1	1	1	0
3	1	1	0	0	1	1	3	1	1	0	1	1	0
4	1	0	1	0	0	0	4	1	0	0	0	1	1
5	0	1	0	0	0	0	5	0	0	1	0	1	1
6	1	0	0	1	1	0	6	0	1	1	1	1	0
7	0	0	9	Ť		1	7	Ł	1	9	Ť		
	-	ndrome		Code word		original ormation			Nonzero		Receiv word		





Example of Systematic Cyclic Code									
Generat	tor polv	nomial	$g(x) = x^4 + x^3 +$	x ² + 1 of (7.	3) code				
Data is 3 bits, $n-k = 4$ bits									
	5 0115, 1	I-K – 4	DIIS						
	Systematic	c (7, 3) Cycl	ic Code Generated by G(x	$x = x^4 + x^3 + x^2 + 1$					
	Message Bit m ₂ m ₁ m ₀		$C(x) = \operatorname{Rem}[x^4M(x) \div G(x)]$	$\begin{tabular}{lllllllllllllllllllllllllllllllllll$					
	000	0	0	0000000					
	001	X ⁴	$x^{3}+x^{2}+1$						
	010	x ⁵	$x^{2}+x+1$	0100111					
	011	x ⁵ +x ⁴	x ³ +x	0111010					
	100	X6	$x^{3}+x^{2}+x$	1001110					
	101	x ⁶ +x ⁴	x+1	1010011					
	110	x ⁶ +x ⁵	x ³ +1	1101001					
	111	x ⁶ +x ⁵ +	x^4 x^2	1110100					
		d(x) x ^{n-k}							
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